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Influence of crossing-beam shoulder and wood species on moment-carrying capacity in a Korean traditional dovetail joint

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Abstract This study investigated the interaction effects of a crossing beam on the moment-carrying capacity of a Korean traditional dovetail joint. In particular, the length of the crossing-beam shoulder (B_s) and the wood species were varied as important factors. Clearly, the B_s acts as a fastener that improves the performance of timber joints by preventing splitting failure parallel to the grain. All the specimens experienced tension failure by tension force in the direction perpendicular to the grain; therefore, the tension strength perpendicular to the grain could be considered an important property, and standard values could be determined to develop a formula for predicting the structural behavior of the joints or the structural design codes of the joints. The results of the tests indicated that the moment resistance of the joints increased as the length of the crossing B_s and the density of the wood species increased. Joint stiffness results also indicated that the joints became stiffer when the crossing beam had shoulders, but the results were not affected by the length of the B_s . In addition, the joint stiffness was proportional to the density of the wood species.

Key words Traditional wooden Korean building · Traditional post-beam joint · Wood-to-wood joint · Dovetail joint · Mortise-and-tenon joint · Moment-carrying capacity · Beam shoulder (B_s) · Wood species

Introduction

Hanok is the traditional Korean wooden building style, and the Korean government recently tried to industrialize and

globalize it with the goal of adding value, boosting the national image, and incorporating traditional cultural elements into everyday lives. Traditional wooden buildings have been constructed based on empirical experience and craftsmanship. The fact that timber has been used as a building material for a long time does not mean that the behavior of the material is scientifically understood. At present, no rational design methods exist pertaining to the engineering of traditional timber frames.

Dovetail joints are commonly used at post-beam joints in traditional Korean wooden buildings. Post-beam joints are critical elements in the analysis of structural behavior. Several researchers^{1–6} have tested the structural performance of the traditional joints, but the behavior of the joint and the factors that affect its performance are still not sufficiently understood. To develop rational design methods, it is foremost necessary to identify the factors that have significant impacts on the joints.

In the upper part of a post, the Korean traditional post-beam joints are composed of three members: post, beam, and *dori* (in Korean), which crosses through the beam. Each of the members is oriented in different directions and jointed on the top of the post (Fig. 1). Pang et al.⁸ investigated the interaction effect of crossing members on the post-beam joints and discovered the effect of the beam shoulder (B_s), but they simply presented the joint performance with or without the B_s . However, not only did the size of the beam shoulder vary according to the builder, but also the joint was commonly made of wood from various species, e.g., Korean red pine (*Pinus densiflora*), Korean pine (*Pinus koraiensis*), and Japanese larch (*Larix kaempferi*). Therefore, to determine an efficient design method, the relationship between the B_s and the joint performance should be ascertained, and the effect of species should be investigated. The study to find the optimized size of the beam shoulder will contribute to the development of standardized sizes for use in modernizing and industrializing Korean traditional wooden joints. The purpose of this study was to investigate the effect of wood density and to discover the relationship between the length of B_s and the moment-carrying capacity in the Korean traditional dovetail joint.

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Materials and methods

Specimens

Seven groups of dovetail joints, with three replications of each, were manufactured using Japanese cedar (*Cryptomeria japonica*, oven-dry density: 353 kg/m³), Douglas fir (*Pseudotsuga menziesii*, oven-dry density: 427 kg/m³), and

Japanese larch (*Larix kaempferi*, oven-dry density: 478 kg/m³) in air-dried conditions (moisture content: 12%–20%).

To identify the test specimens, joint IDs were established according to the species of wood, the post width (P_w), and the beam width (B_w), as shown in Fig. 2. For example, the joint ID C-180-60 in Table 1 indicates that the species of the joint is Japanese cedar, the P_w is 180 mm, and the B_w is 60 mm. A joint ID of C-180-180 means that the wood species and P_w are the same as for C-180-60, and B_w is 180 mm, so that the mortise branches are fully covered by the B_s .

Figure 3 shows how the three members are combined on top of a post; Figs 3a,b show the configuration of the dovetail joint before and after combining the three members, respectively. As shown in Fig. 3c, the B_w of C-180-60 was 60 mm, and the specimen did not have a B_s (0 mm). In contrast, the B_w of C-180-180 was 180 mm, and the B_s (60 mm) fully covered the mortise branches. As the B_w increases in increments of 30 mm (such as C-180-90, C-180-120, and C-180-150), the B_s increases in increments of 15 mm. In other words, the ratios of the length of the B_s in joint configurations from C-180-60 to C-180-180 are 0:0.25:0.5:0.75:1.

To determine the influence of the B_s , B_w alone was changed while the other dimensions of the beam, post, and *dori* were kept the same (Fig. 4). Regarding the size of the dovetailed tenon on the *dori*, the length of the tenon was the same as the length of the mortise branch on the post, the neck of the tenon was one-third of the *dori* width (180 mm), and the head of the tenon was 1.5 times larger than its neck. Therefore, the angle of the dovetailed tenon (α) was approximately 1.32 radians according to Eq. 1. In addition, both the depth of the dovetailed tenon and the beam depth were the same as the *dori* depth.

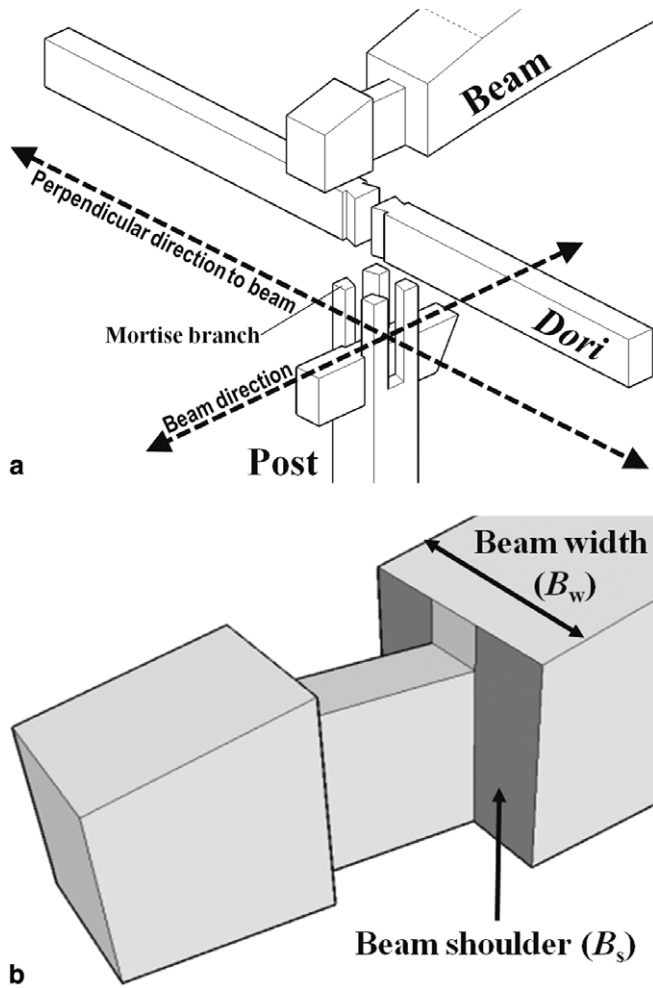


Fig. 1a–b. Korean traditional dovetail joint. **a** Two members, the beam and *dori*, are jointed on top of the post; **b** the contact surface between beam shoulders and mortise branches of the post increases as the beam width increases

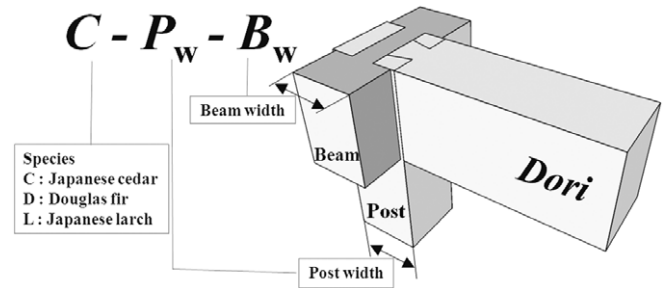


Fig. 2. The joint ID for test specimens is made up of a species identifier, the post width, and the beam width

Table 1. Ratios of moment-carrying capacity depending on the beam shoulder length

	Joint ID	L_{Bs} (mm)	M_{max} (kN·m)		M_y (kN·m)		K_i (kN·m/rad.)		Failure mode
			Average	R_e	Average	R_e	Average	R_e	
a	C-180-60	0	0.75	0.31	0.41	0.28	5.08	0.45	Top of the post
b	C-180-90	15	1.56	0.65	0.90	0.62	10.63	0.94	Mortise branch
c	C-180-120	30	1.86	0.77	1.27	0.87	12.78	1.13	Mortise branch
d	C-180-150	45	2.04	0.85	1.24	0.86	16.65	1.48	Beam shoulder
e	C-180-180	60	2.40	1.00	1.45	1.00	11.26	1.00	Beam shoulder

L_{Bs} , the length of beam shoulder; M_{max} , maximum moment; M_y , yield moment; K_i , initial stiffness; R_e , the ratio of a, b, c, and d to e

Fig. 3a–c. The configuration of a dovetail joint. **a** Before combining the members; **b** after combining the members; **c** the length of the beam shoulder in each specimen

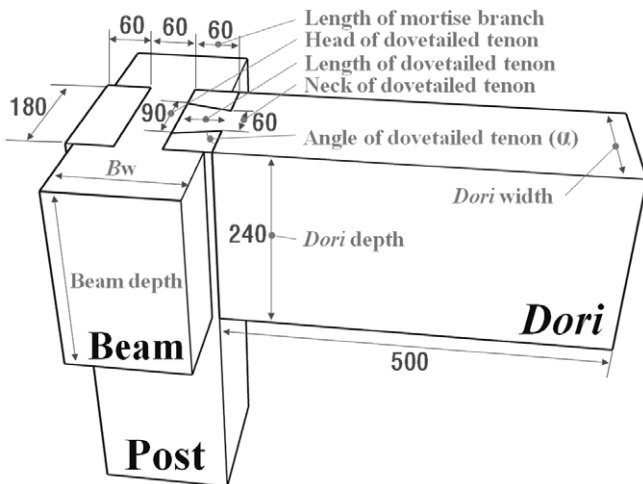
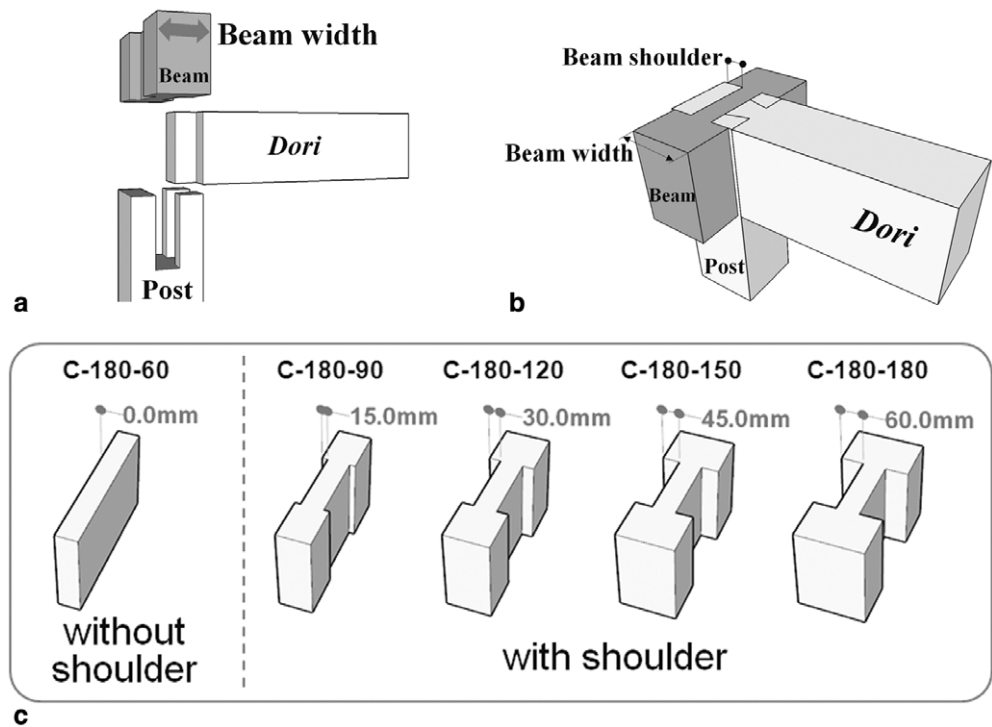


Fig. 4. The dimensions of specimens for testing the effect of the beam shoulder. Only the beam width (B_w) was changed, the other dimensions of the beam and both the post and *dori* were controlled with uniform shape and size

$$\alpha = \arctan[L/\{(H - N)/2\}] \quad (1)$$

where α is the angle of the dovetailed tenon, L is the length of dovetailed tenon (60 mm), H is the head of dovetailed tenon (90 mm), N is the neck of dovetailed tenon (60 mm).

Experimental procedures

In order to investigate the moment–rotation characteristics and failure modes of dovetail joints, specimens were supported in a universal testing machine (Zwick) by means of

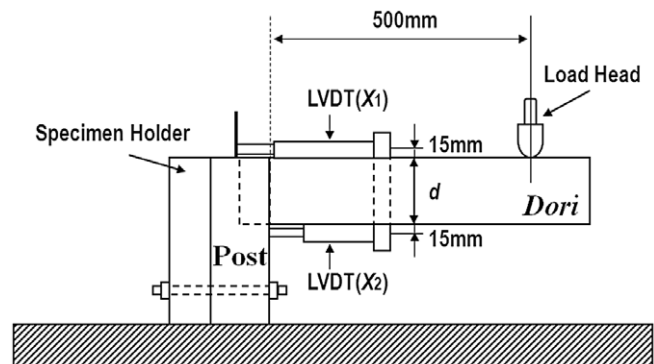


Fig. 5. Diagram of the setup used to test the specimens.⁹ LVDT, linear variable differential transformer

the jig shown in Figs. 5 and 6. The load head speed was 5 mm/min. Measurements of joint flexibility were obtained by means of a linear variable differential transformer (LVDT) placed on the top edge of the *dori*. Testing continued until the applied load stopped increasing or until the occurrence of an obvious joint failure with a sudden falloff in load.

The internal joint rotation angle (θ) was calculated using the displacement of both LVDT (x_1) and LVDT (x_2), as well as the distance between LVDT (x_1) and LVDT (x_2). By the geometric relationship between the joint rotation angle and displacements, as shown in Fig. 7, Eq. 2 can be obtained:

$$\theta = \arctan[(X_1 + X_2)/(15 + d + 15)] \quad (2)$$

where X_1 is the displacement of LVDT (x_1), measured on the top side of the *dori*; X_2 is the displacement of LVDT



Fig. 6. Test setup for evaluating the moment-carrying capacity of dovetail joints

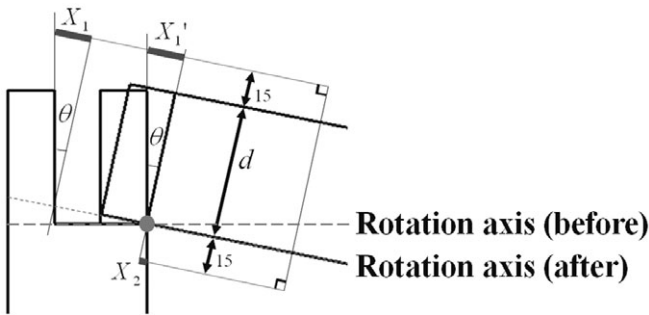


Fig. 7. Geometric relationship between joint rotation angle and displacement

(x_2), measured on the bottom side of the *dori*; and $15 + d + 15$ is the distance between the two LVDTs, where d is the depth of the *dori*.

Definition of the strength properties of the joints

The definitions and a method for calculating the strength properties of mechanical timber joints are shown in Fig. 8. The calculation was performed as follows:^{10–12}

1. Line I, a straight line that connects $0.1 M_{\max}$ and $0.4 M_{\max}$ in the moment–deflection angle curve (where M_{\max} denotes the maximum moment), was drawn.
2. Line II, a straight line that connects $0.4 M_{\max}$ and $0.9 M_{\max}$ in the curve, was drawn.
3. Line II was offset in the x -axis direction in order to create a line tangent to the curve. This new line was defined as line III.
4. The moment corresponding to the intersection of lines I and III was defined as the yield moment (M_y). Line IV was drawn parallel to the x -axis through this point.
5. The deflection angle corresponding to the intersection of line IV and the curve was defined as the yield deflection angle (θ_y).

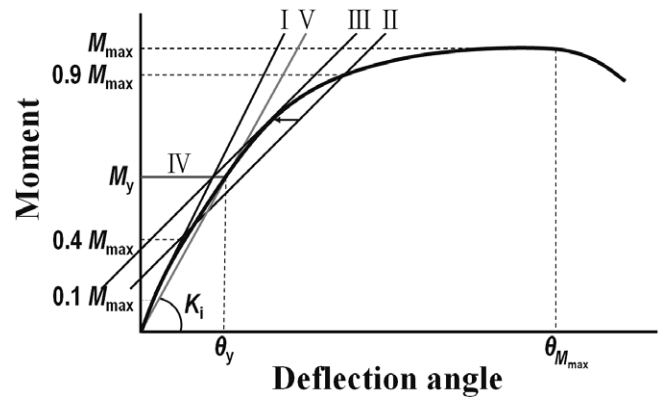


Fig. 8. Definition of the joint's performance. M_{\max} , maximum moment; M_y , yield moment; K_i , initial stiffness; θ_y , yield angle; $\theta_{M_{\max}}$, deflection angle at maximum moment. The determination of lines I–V is given in the text

6. Line V, the straight line that connects the origin and the coordinates (M_y, θ_y) was drawn. The slope of this line was defined as the initial stiffness (K_i) and was calculated using Eq. 3:

$$\text{Initial stiffness } (K_i) = M_y / \theta_y \text{ (kN} \cdot \text{m/rad.)} \quad (3)$$

Results and discussion

Influence of beam shoulder on failure modes

The failure modes of the specimens in this test differed depending on the length of the B_s and B_w , as shown in Fig. 9. For specimens without a B_s (C-180-60, B_w : 60, length of B_s : 0 mm), the gap between the mortise branches widened as the moment increased, as shown in Fig. 9a, and tension failures occurred on top of the post, as shown in Fig. 9b. However, for specimens with a B_s , shear failures of the mortise branches (C-180-90 and C-180-120) or tension failures of the B_s (C-180-150 and C-180-180) occurred. It can be considered that the presence of a B_s prevented mortise branches from moving outward and resulted in the different failure modes.

Joint rotation occurred due to the vertical load (F), as shown in Fig. 10a, and the mortise branch moved outward by the angle of the dovetailed tenon (α), as shown in Fig. 10b. This mechanism appeared in the case of specimens without a B_s and the behavior of the mortise branch caused a tension force perpendicular to the grain on the post, and the tension failure was checked on top of the post. In the case of specimens with a B_s , when the length of the B_s was 15–30 mm, the B_s prevented this behavior of the mortise branches. As the movement of the mortise branches was prevented, friction occurred between the dovetailed tenon and mortise branches, and rolling shear failures appeared at the mortise branches due to shear force between the dovetailed tenon and B_s , as shown in Fig. 10c. When the length of the B_s was increased to 45–60 mm, tension failures occurred at the B_s on the beam instead of rolling shear

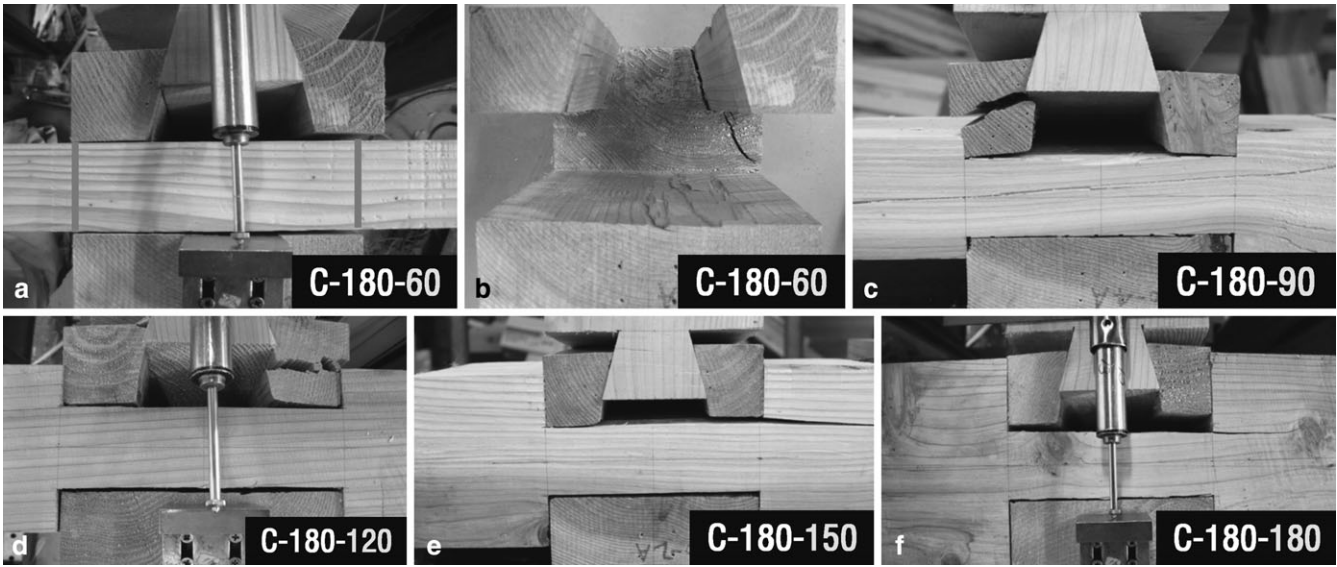


Fig. 9a–f. Failure modes of dovetail joints in the test. **a** The mortise branch moves outward; **b** split failure parallel to the grain at the post; **c,d** rolling shear failure at the mortise branch; **e,f** split failure parallel to the grain at the beam shoulder on the beam

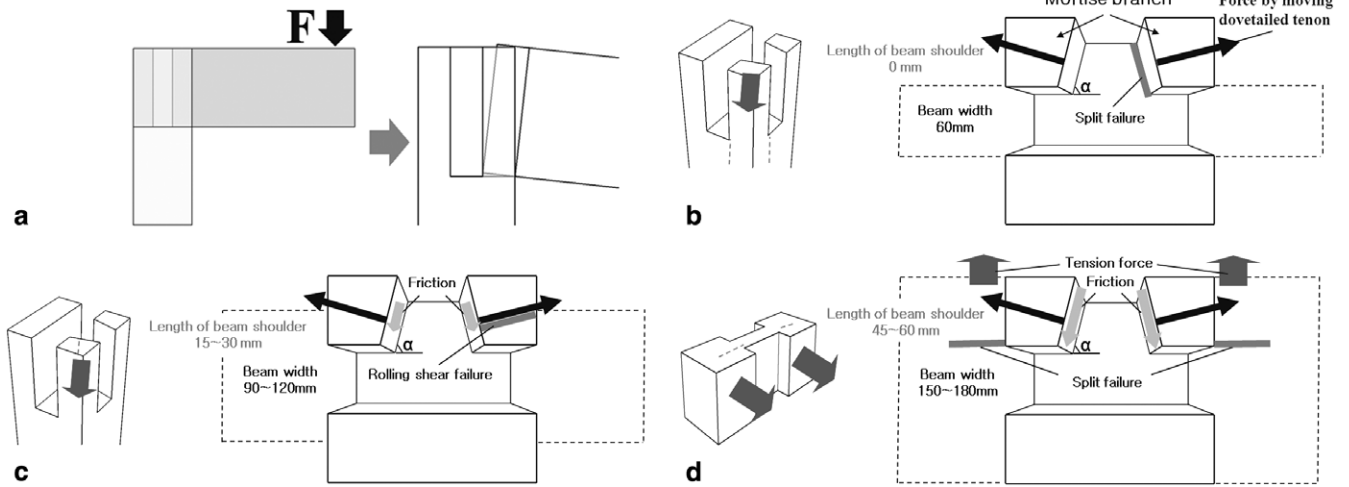


Fig. 10a–d. Diagrams of failure modes depending on the length of the beam shoulder. **a** Behavior of the dovetail joint; **b** split failure parallel to the grain at the post, where α is the angle of the dovetailed

tenon; **c** rolling shear failure parallel to the grain at the mortise branch; **d** split failure parallel to the grain at the beam shoulder on the beam

failure at the mortise branches. As both mortise branches moved outward, the B_s also moved outward with the mortise branches, and a tension force occurred at the B_s on the beam, as shown in Fig. 10d.

The phenomena in which the different failure modes occur can be explained by friction as shown in Fig. 11, and the friction can be expressed as Coulomb friction as follows:

$$F_n \leq \mu N_n \quad (4)$$

where F_n is the force exerted by friction; μ is the coefficient of friction, which is an empirical property of the contacting materials; and N_n is the normal force exerted between the surfaces.

When a B_s is present, frictional forces F_{Bs} (between B_s and the mortise branch) and F_{Mb} (between the mortise

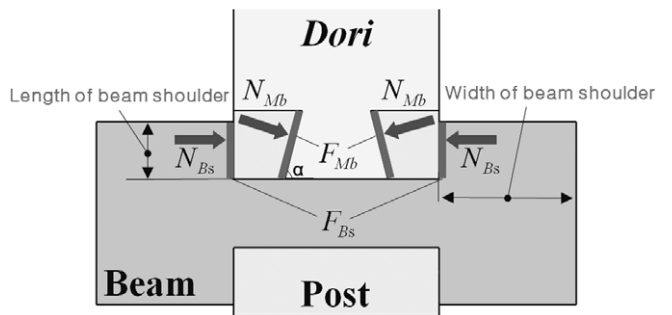


Fig. 11. Friction diagram. N_{Bs} , normal force between beam shoulder and mortise branch; N_{Mb} , normal force between mortise branch and dovetailed tenon; F_{Bs} , frictional force between beam shoulder and mortise branch; F_{Mb} , frictional force between mortise branch and dovetailed tenon

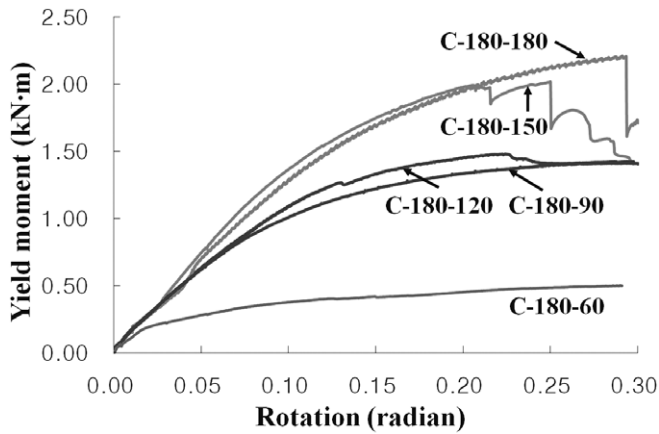


Fig. 12. The moment–rotation curve. C-180-60, split failure occurred at the post; C-180-90 and C-180-120, rolling shear failure occurred at the mortise branch; C-180-150 and C-180-180, split failure occurred at the beam shoulder on the beam

branch and dovetailed tenon on the *dori*) occur due to the length of B_s and the normal forces N_{Bs} (between B_s and the mortise branch) and N_{Mb} (between the mortise branch and dovetailed tenon on the *dori*), perpendicular to the surface of contact. The contact surfaces between the B_s and the mortise branch increase as the length of B_s increases, and the normal forces (N_{Bs} and N_{Mb}) also increase because the movement of the mortise branches is prevented by the B_s .

If movement of the dovetailed tenon causes N_{Mb} to exceed the rolling shear resistance of the mortise branch, then rolling shear failure appears, as shown in Fig. 10c. If the B_s (Fig. 11) is not sufficiently wide and N_{Bs} is greater than the shear resistance of the B_s on the beam, then shear failure appears in the B_s on the beam instead of split failure caused by the tension force. In this study, the width of the B_s was 120 mm and shear failure of the B_s did not occur; however, both the width and length of the B_s are important to consider.

As a result, the B_s acts as a fastener^{13–15} that improves the performance of timber joints by preventing splitting failure parallel to the grain. In addition, the friction between the dovetailed tenon and mortise branches increases as the length of the B_s increases.

Influence of beam shoulder on moment-carrying capacity

The moment–rotation curves (Fig. 12) show that the effect of the B_s was also evident in the moment capacity and the initial stiffness. Both the moment capacity and the initial stiffness varied depending on the absence or presence of a B_s . In addition, for joints with a B_s , the maximum moment (M_{max}) increased as the length of the B_s increased (Fig. 13), and the yield moment (M_y) also tended to increase as the length of the B_s increased (Fig. 14). The tendency of the moment also increased, depending on the length of the B_s . The relationship between M_{max} and the length of the B_s was similar to that between M_y and the length of the B_s . There-

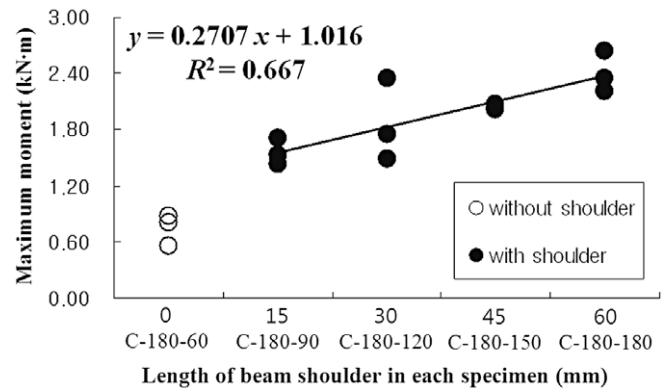


Fig. 13. Relationship between the length of the beam shoulder (B_s) and the maximum moment (M_{max})

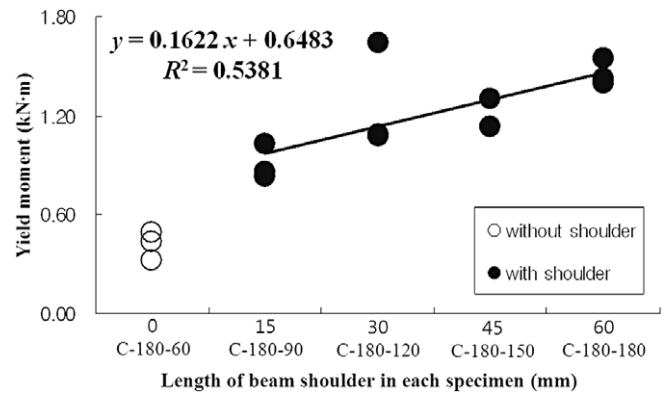


Fig. 14. Relationship between the length of the B_s and the yield moment (M_y)

fore, the yield moment depends on the maximum moment and the failure modes related to the maximum moment.

The difference in mechanical properties depending on the length of the B_s seems to be caused by friction affecting the different failure modes, as shown in Fig. 11. In other words, the friction force increased due to the fixed mortise branches and this improved both the moment capacity and the initial stiffness. This means that the friction reinforced by the B_s affects the failure modes and increases the moment capacity.

The initial stiffness (K_i) also varied depending on the absence or presence of the B_s . However, in the presence of a B_s , initial stiffness did not tend to increase as the length of the B_s increased, as shown in Fig. 15. However, the maximum and yield moments tended to increase as the length of the B_s increased. The initial stiffness was affected by the absence or presence of a B_s , but was not affected by its length.

Table 1 shows the properties, the maximum moment (M_{max}), the yield moment (M_y), and the initial stiffness (K_i) values of each specimen. R_c values represent the ratios of the values of each specimen to those of C-180-180, in which the mortise branches are fully covered by the B_s . For example, the M_{max} values of C-180-60 specimens (without a B_s) averaged 31% of the corresponding values of C-180-180

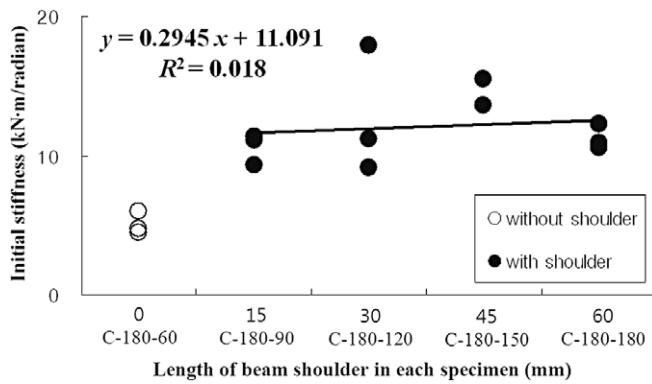


Fig. 15. Relationship between the length of the B_s and the initial stiffness (K_i)

specimens, and M_y values were approximately 28% those of C-180-180. The ratios of M_{max} and M_y for joints increased as the length of the B_s increased. Meanwhile, although the average K_i of C-180-60 was about 45% that of C-180-180, the average K_i for C-180-90 (which has a B_s length of 15 mm) averaged 94% that of C-180-180. When the length of the B_s was 30 or 45 mm, the average K_i exceeded the average K_i of C-180-180. Therefore, the K_i of specimens with a B_s was distinct from the specimens without a B_s , and the K_i of dovetail joints could be reinforced by the B_s , even when a beam had a short B_s .

Wood species versus mechanical properties of dovetail joints

The mortise branches of specimens used to investigate the effect of wood species were fully covered with the B_s (i.e., B_w was 180 mm), and the failure modes of specimens were the same regardless of species. All specimens failed at the B_s on the beam, and tension failure by tension force perpendicular to the grain occurred, as shown in Figs. 9f and 10d.

The effect of density with respect to species was clarified in the relationship with joint stiffness and moment capacity. Density was measured at the part nearest to the failure. Initial stiffness (K_i) was proportional to the density, as shown in Fig. 16. The maximum moment (M_{max}) and yield moment (M_y) were also proportional to the density, as shown in Figs. 17 and 18. However, the gradients of the density- M_{max} and density- M_y relationships were lower than the gradient of the density- K_i relationship.

It could be considered that the moment capacity was influenced by the failures. Moment capacity is clearly closely related to failures, and so tension failures by tension force perpendicular to the grain were investigated. In fact, tension strength perpendicular to the grain is highly related to the cleavage strength, which is the lowest strength property of wood, as well as having the lowest difference between species of any property according to data from previous studies.¹⁶⁻¹⁸ As a result, it seems that the M_{max} and M_y values were less influenced than the K_i values were by the wood density, due to the cleavage resistance.

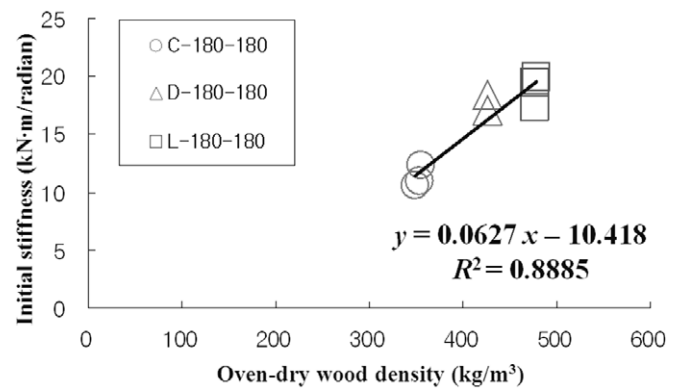


Fig. 16. Relationship between wood density and initial stiffness (K_i)

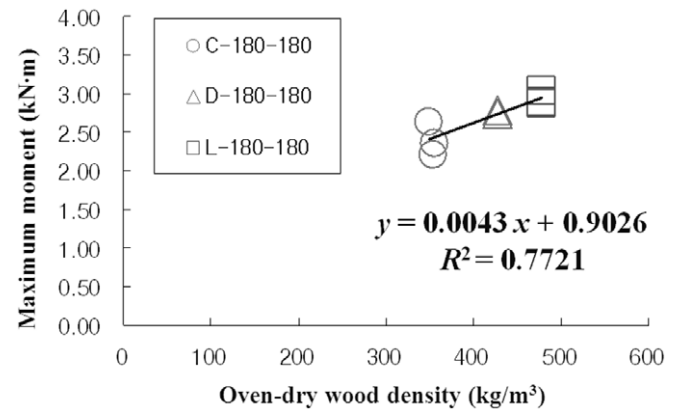


Fig. 17. Relationship between wood density and maximum moment (M_{max})

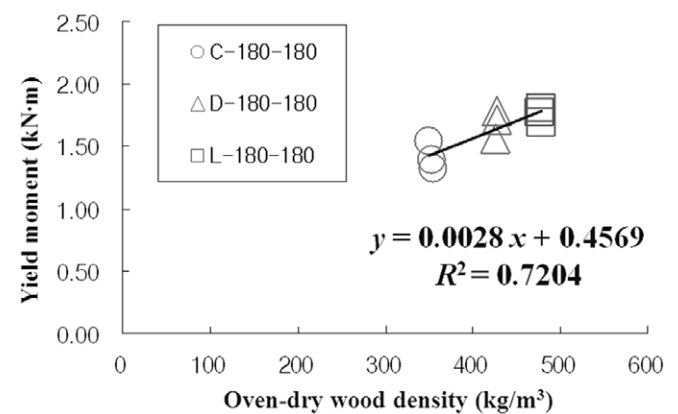


Fig. 18. Relationship between wood density and yield moment (M_y)

In Table 2, R_c shows the ratios of the properties for each specimen to those of L-180-180 (Japanese larch) specimens. C-180-180 (Japanese cedar) joints had approximately 83% of the M_y and 60% of the K_i of Japanese larch. D-180-180 joints (Douglas fir) had about 96% of the M_y and 93% of the K_i of the equivalent joint made from Japanese larch. These results indicate that K_i was more affected by the

Table 2. Ratios of moment-carrying capacity depending on wood species

	Joint ID	Species	Oven-dry density (kg/m ³)	M_{max} (kN·m)		M_y (kN·m)		K_i (kN·m/rad)	
				Average	R_c	Average	R_c	Average	R_c
a	C-180-180	Japanese cedar	353	2.40	0.82	1.45	0.83	11.26	0.60
b	D-180-180	Douglas fir	427	2.76	0.94	1.69	0.96	17.45	0.93
c	L-180-180	Japanese larch	478	2.94	1.00	1.76	1.00	18.86	1.00

M_{max} , maximum moment; M_y , yield moment; K_i , initial stiffness; R_c , the ratio of a and b to c

wood species than the other parameters were. Therefore, the wood species should be considered as a factor in the structural design of a dovetail joint.

Conclusions

The experimental results regarding failure modes and moment resistance indicated that the length of the B_s and the wood species significantly affected the performance of Korean traditional dovetail joints; it was clear that the B_s acts as a fastener that improves the performance of timber joints by preventing splitting failure parallel to the grain.

For all failure modes, the failures occurred by tension force perpendicular to the grain. Therefore, the tension strength perpendicular to the grain is an important property and can be determined as standard values to develop a formula for predicting the structural behavior of the joints or the structural design codes of the joints.

The moment resistance of the joints was affected by the B_s length and became higher as the length increased. Joint stiffness results also indicated that the joints stiffened when the beam had a B_s , but were not affected by its length. The joint stiffness and moment resistance were proportional to the density of the wood species, but the moment resistance tended to be less sensitive to the wood density than the joint stiffness was.

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